Quantum Information Science (QIS)

Dr. Boris Kiefer, Lecture 1

Quantum Computing Quantum Communication Quantum Sensing

QIS exploits quantum principles to transform how information is acquired, encoded, manipulated, and applied. QIS encompasses quantum computing, quantum communication, and quantum sensing.

- 1. QIS employs quantum mechanics, a well-tested theory that uses the mathematics of probability, vectors, algebra, and linear transformations to describe the physical world.
- 2. QIS combines information theory and computer science.
- 3. QIS demonstrated impact on high-impact technologies, such as GPS which depends on the extreme precision of atomic clocks.

What have we learned so far?

- Quantum States.
- Measurements.
- Qubits.
- Entanglement.
- Decoherence.
- Quantum Computers.
- Quantum Communication.
- Quantum Sensing.

• Quantum States.

A quantum state is a mathematical representation of a physical system, such as an atom, and provides the basis for processing quantum information.

1. Quantum states are represented by vectors in an abstract space,

$$\begin{split} |0>,|1> \\ |\Psi> = a_0 |0> + a_1 |1>; a_0^2 + a_1^2 = 1 \end{split}$$

2. The direction of a quantum state vector determines the probabilities of all possible outcomes of a measurement. This captures a behavior that cannot solely be captured by the arthimetic of probability.

$$|\Psi\rangle = |a_0|0\rangle + a_1|1\rangle; a_0^2 + a_1^2 = 1$$

• Quantum States.

3. Quantum systems are fragile. For instance, measurement almost always disturbs a quantum system in a way that cannot be ignored. This fragility influences the design of computational algorithms, communication, and sensing protocols. For example, the orientation of the state vector be-

fore and after measurement may differ: projection erases any non-parallel components to the state vector after measurement. May be one of the most succinct expressions of this statement is the Heisenberg uncertainty principle, for applied to position and linear momentum (p = mv):

$$\Delta x \cdot \Delta p \ge \frac{\hbar}{2}$$

Therefore, the smaller the desired uncertainty in location (smaller Δx), the larger the corresponding uncertainty in momentum (Δp , direction and magnitude).

• Measurements.

Quantum applications are designed to carefully manipulate fragile quantum systems without observation to increase the probability htat the final measurement will provide the intended result.

- 1. A measurement is an interaction with the quantum system that transforms a state with multiple possible outcomes into a "collapsed" state that now has only one outcome: the measured outcome.
- 2. A quantum state determines the probability of the outcome of a single quantum measurement, but one outcome rarely reveals complete information of the system.
- 3. Repeated measurements on identically prepared quantum systems are required to determin more complete information about the (quantum) state.
- 4. Because of the limitations of quantum measurements (providing only partial information and disturbing the sysyem), quantum states cannot be copies or duplicated.

• Measurement.

$$|\Psi\rangle = |a_0|0\rangle + a_1|1\rangle; a_0^2 + a_1^2 = 1$$

and the probability to observe the system in one of the two possible states is:

 $|0>:|a_0|^2$ $|1>:|a_1|^2$

$$M_0 = |0> < 0|$$

$$Pr[|0>] = |M_0|\Psi>|^2 = <\Psi|M_0^{\dagger}M_0|\Psi>$$

with results in the new quantum state:

$$|\Psi'\rangle = \frac{M_0|\Psi\rangle}{\sqrt{\langle\Psi|M_0^{\dagger}M_0|\Psi\rangle}}$$

• Qubits.

The qubit is the fundamental unit of quantum information, and is encoded in a physical system, such as polarization states of light, energy states of an atom, or spin states of an electron.

- 1. Unlike a classical bit, a qubit represents information in a superposition, or vector sum that incorporates two mutually exclusive quantum states.
- 2. At a particular moment in time a, a set of N classical bits can only exist in 2^N possible states, but a set of N qubits can exist in a superposition of all these states. This capability allows quantum information to be stored and processed in ways that would be difficult or impossible to do classically.
- 3. Multiple qubits can be entangled, where the measurement outcome of one qubit is correlated with the measurement outcomes of the others.

• Qubits.

Example: 3 Qubit States:

$$\left(\begin{array}{c}0\\0\\0\end{array}\right), \left(\begin{array}{c}0\\1\\1\end{array}\right), \left(\begin{array}{c}0\\1\\0\end{array}\right), \left(\begin{array}{c}0\\1\\1\end{array}\right), \left(\begin{array}{c}0\\1\\1\end{array}\right), \left(\begin{array}{c}1\\0\\0\end{array}\right), \left(\begin{array}{c}1\\0\\1\end{array}\right), \left(\begin{array}{c}1\\1\\0\end{array}\right), \left(\begin{array}{c}1\\1\\1\end{array}\right)$$

In the quantum mechanical version, linear combination of these states are allowed:

$$a_0 \begin{pmatrix} 0\\0\\0 \end{pmatrix} + a_1 \begin{pmatrix} 0\\0\\1 \end{pmatrix} + a_2 \begin{pmatrix} 0\\1\\0 \end{pmatrix} + a_3 \begin{pmatrix} 0\\1\\1 \end{pmatrix} + a_4 \begin{pmatrix} 1\\0\\0 \end{pmatrix} + a_5 \begin{pmatrix} 1\\0\\1 \end{pmatrix} + a_6 \begin{pmatrix} 1\\1\\0 \end{pmatrix} + a \begin{pmatrix} 1\\1\\1 \end{pmatrix} + a \begin{pmatrix} 1\\1\\1 \end{pmatrix} \sum |a_i|^2 = 1$$

• Entanglement

Entanglement, an inseperable relationship between multiple qubits, is a key property of quantum systems necessary for obtaining a quantum advantage in most QIS applications.

- 1. When multiple quantum system in superposition are entangled, their measuremnts outcomes are correlated. Entanglement can cause correlations that are different from what is possible in classical systems.
- 2. An entangled quantum system of multipl equbits cannot be described solely by specifying a an individual quantum state for each qubit.
- 3. Quantum technologies rely on entanglement in different ways. When a fragile entangled state is maintained, a computational advantage can be realized. The extreme sensitivity of entangled states, however, can enhance sensing and communication.

• Entanglement: Bell States

$$|\Phi^+> = \frac{1}{\sqrt{2}} \left(|00> + |11>\right)$$

Let's try to write this as a tensor product of two single qubits: $a_0b_0 = \frac{1}{\sqrt{2}}$ $a_1b_0 = 0$ $a_0b_1 = 0$ $a_0b_1 = 0$ $a_0b_1 = 0$ $a_1b_1 = \frac{1}{\sqrt{2}}$ $|a > \otimes |b >= a_0b_0|00 > +a_1b_0|10 > +a_0b_1|01 > +a_1b_1|11 >$

and we compare the coefficients, one-by-one:

• Entanglement: Bell States

$$\begin{split} |\Phi^+> &= \frac{1}{\sqrt{2}} \left(|00>+|11>\right) \\ |\Phi^-> &= \frac{1}{\sqrt{2}} \left(|00>-|11>\right) \\ |\Psi^+> &= \frac{1}{\sqrt{2}} \left(|01>+|10>\right) \\ |\Psi^-> &= \frac{1}{\sqrt{2}} \left(|01>-|10>\right) \end{split}$$

Entangled States realize state correlations between quantum objects, regardless of distance: Teleportation,...

Therefore, the question arises how to generate an entangled state?

• Entanglement: Creating a Bell State

Therefore, the question arises how to generate an entangled state? Let's assume

that we can initialize a unique state, say $|0\rangle$. First we generate a superposition state by applying a Hadamard gate to this state:

$$\begin{split} |s>=H|0>\\ =\frac{1}{\sqrt{2}}\left(|0><0|+|1><0|+|0><1|+|1><1|\right)|0>\\ &\quad \frac{1}{\sqrt{2}}\left(|0>+|1>\right) \end{split}$$

or in matrix notation:

$$\frac{1}{\sqrt{2}} \left(\begin{array}{cc} 1 & 1 \\ 1 & -1 \end{array} \right) \left(\begin{array}{c} 1 \\ 0 \end{array} \right) = \frac{1}{\sqrt{2}} \left(\begin{array}{c} 1 \\ 1 \end{array} \right)$$



• Entanglement: Creating a Bell State



now we have to apply a "disruptive" step that entangles this state with a welldefined second qubit, that we assume to be in state $|0\rangle$. So, the current state of the system is:

$$\frac{1}{\sqrt{2}} \left(|0>+|1> \right) \otimes |0> = \frac{1}{\sqrt{2}} \left(|00>+|10> \right)$$

Since this state was generated as a tensor product, it is clearly not entangled. How does this state transform if we apply a CNOT operation:

$$\begin{split} X &= |1> < 0| + |0> < 1| \\ CNOT &= |0> < 0| \otimes I + |1> < 1| \otimes X \\ &= |0> < 0| \otimes (0> < 0| + |1> < 1|) + |1> < 1| \otimes (1> < 0| + |0> < 1|) \\ &= |00> < 00| + |01> < 01| + |11> < 10| + |10> < 11| \end{split}$$

and the action of CNOT can easily be read off from the last equation:

• Entanglement: Creating a Bell State

and the action of CNOT can easily be read off from the last equation:

 $\begin{array}{l} |00>\rightarrow |00>\\ |01>\rightarrow |01>\\ |10>\rightarrow |11>\\ |11>\rightarrow |10> \end{array}$

and the matrix representation is of CNOT is:

 $\left(\begin{array}{rrrrr}1&0&0&0\\0&1&0&0\\0&0&0&1\\0&0&1&0\end{array}\right)$

Now, we can apply CNOT to our superposition state:

$$CNOT\left(\frac{1}{\sqrt{2}}\left(|00>+|10>\right)\right)$$
$$=\frac{1}{\sqrt{2}}\left(|00>+|11>\right)=|\Phi^{+}>$$

Entangled State = CNOT * Hadamard * |0>

(Standard procedure after initialization of qubits to create entangled states).

• Decoherence.

For quantum information applications to be successfully completed, fragile quantum states must be preserved, or kept coherent.

- 1. Decoherence erodes superposition and entanglement of undesired interacton with the surrounding environment. Uncontrolled radiation, inclusing light, vibration, heat, or magnetic fields, can all cause decoherence.
- 2. Some types of qubits are inherently isolated, whereas others require carefully engineered materials to maintain their coherence.
- 3. High decoherence rates limit the length and complexity of quantum computations; implementing methods that corect errors can mitigate these errors.

• Quantum Computers.

Quantum computers, which use qubits and quantum operations, will solve certain complex computational problems for efficiently than calssical computers.

- 1. Qubits can represent information compactly; more information can be stored and processed using 100 qubits than the largest conceivable classical supercomputer.
- 2. Quantum data can be kept in a superprosition of exponentially many classical states during processing, giving quantum computers a significant speed advantage for certain computations such as factoring large numbers (exponential speed-up) and performing searches (quadratic speed-up). However, there is no speed advantage for many other types of computations.
- 3. A fault tolerant quantum computer corrects all errors that occur during quantum computation, inclusing those arising from decoherence, but error correction requires significantly more resources than the original computation.

• Quantum Computers – Gates, s gate: rotates the

GATE	CIRCUIT REPRESENTATION	MATRIX REPRESENTATION	TRUTH TABLE	BLOCH SPHERE
I Identity-gate: no rotation is performed.	[]	$I = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{array}{c c} \underline{\text{Input}} & \underline{\text{Output}} \\ \hline 0\rangle & \hline 0\rangle \\ 1\rangle & 1\rangle \end{array}$	x x
X gate: rotates the qubit state by π radians (180°) about the x-axis.	— <u>X</u> —	$X = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{array}{c c} Input \\ 0\rangle \\ 1\rangle \\ 1\rangle \\ 0\rangle \end{array}$	z 1809 x
Y gate: rotates the qubit state by π radians (180°) about the y-axis.	— <u>Y</u> —	$Y = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}$	Input Output 0⟩ i 1⟩ 1⟩ -i 0⟩	x x x x x x x x x x x x x x x x x x x
Z gate: rotates the qubit state by π radians (180°) about the z-axis.	— Z —	$Z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{array}{c c} \hline \text{Input} \\ \hline 0\rangle \\ \hline 0\rangle \\ \hline 1\rangle \\ \hline - 1\rangle \end{array}$	x y



GATE	CIRCUIT REPRESENTATION	MATRIX REPRESENTATION	TRUTH TABLE
Controlled-NOT gate: apply an X-gate to the target qubit if the control qubit is in state 1〉		$CNOT = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix}$	$\begin{array}{c c} Input \\ 00\rangle \\ 01\rangle \\ 10\rangle \\ 11\rangle \\ 10\rangle \\ 10\rangle \end{array} \begin{array}{c} Output \\ 00\rangle \\ 01\rangle \\ 11\rangle \\ 11\rangle \end{array}$
Controlled-phase gate: apply a Z-gate to the target qubit if the control qubit is in state 1>	Z	$CPHASE = \left(\begin{array}{rrrr} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{array}\right)$	$\begin{array}{c c} \mbox{Input} & \mbox{Output} \\ \hline \mbox{ 00\rangle} & \mbox{ 00\rangle} \\ \mbox{ 01\rangle} & \mbox{ 01\rangle} \\ \mbox{ 10\rangle} & \mbox{ 10\rangle} \\ \mbox{ 11\rangle} & -\mbox{ 11\rangle} \end{array}$

• Quantum Computers – Universal Gate Sets

A common universal quantum gate set is

$$\mathcal{G}_0 = \{ \mathsf{X}_\theta, \mathsf{Y}_\theta, \mathsf{Z}_\theta, \mathsf{Ph}_\theta, \mathsf{CNOT} \}$$
(71)

where $Ph_{\theta} = e^{i\theta} \mathbb{1}$ applies an overall phase θ to a single qubit. For completeness we mention another universal gate set which is of particular interest from a theoretical perspective, namely

$$\mathcal{G}_1 = \{\mathsf{H}, \mathsf{S}, \mathsf{T}, \mathsf{CNOT}\},\tag{72}$$

Krantz et al. (2019)

• Quantum Communication.

Quantum communication uses entanglement or a transision channel, such as a optical fiber, to transfer quantum information between different locations.

- 1. Quantum teleprotation is a protocol that uses entanglement to destroy quantum information at one location and and recreate it at a second site, without transferring physical qubits.
- 2. Quantum cryptography enhances provacy based on quantum physical principles and cannot be circumvented. Due to the fragility of quantum systems, an eavesdropper's interloping measurement will almost always be detected.

Quantum Sensing.

Quantum sensing uses quantum states to detect and measure physical properties with the highest precision allowed by quantum mechanics.

- 1. The Heisenberg uncertainty principle describes a fundamental limit in simultaneous measureing two specific, separate attributes. "Squeezing" deliberatly sacrifices the certainty of measuring one attribute in order to achieve higher precision in measureing the other attribute; for example squeezing is used in LIGO to improve the sensitivity to gravitational waves.
- 2. Quantum sensors take advantage of the fact that physical qubits are extremely sensitive their surroundings. The same fragility that leads to rapid decoherence enables precise sensors. Examples include magnetometers, single-photon detectors, and atomic clocks for improvement of medical imaging, navigation, position, and timing.
- 3. Quantum sensing has vastly improved the precision and accuracy of measuremnts of fundamental constants, freeing the International System of Units from its dependence on one-of-a-kind artifacts. Measurement units are now defined through these fundamental constants, like the speed of light and Planck's constant.

Chapter 13.7: (The Physics and Engineering Behind) Building Quantum Computers

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From Concept to (Quantum)Computer

DiVincenzo criteria for qubit design (DiVincenzo, 2000):

- Scalable system with well-characterized qubits.
- Ability to initialize qubits.
- Stability of qubits.
- Support of universal computation.
- Ability to measure qubits.

From Concept to (Quantum)Computer

$$H|\psi > E|\psi >$$
$$|\psi(x,t) >= e^{-\frac{i\dot{H}t}{\hbar}}|\psi(x,0) >$$



Google: Sycamore processor



SNL: ion trap

https://ai.googleblog.com/2019/10/quantum-supremacyusing-programmable.html

https://www.sandia.gov/quantum/

Quantum Mechanical Objects

Quantization energy states.

Spin: No classical analog Electronic, nuclear, defects...

Time evolution: unitary operator.

Superconductivity: Macroscopic Quantum States. Cooper-pairs. Josephson Junction.

In general: Low Temperatures.





A bit of the action

In the race to build a quantum computer, companies are pursuing many types of quantum bits, or qubits, each with its own strengths and weaknesses.



Note: Longevity is the record coherence time for a single qubit superposition state, logic success rate is the maximum number of qubits entangled and capable of performing two-qubit operations.

Quantum – LC Circuit

Low temperature



$$egin{aligned} \phi &
ightarrow \hat{\phi} \ q &
ightarrow \hat{q} \ H &
ightarrow \hat{H} = rac{{\hat{\phi}}^2}{2L} + rac{{\hat{q}}^2}{2C} \end{aligned}$$

and enforcing the canonical commutation relation

$$\left[\hat{\phi}, \hat{q}
ight] = i \hbar$$

$$H=rac{\phi^2}{2L}+rac{1}{2}L\omega^2Q^2$$

where Q is the charge operator, and ϕ is the represents the energy stored in a capacitor. independent Schrödinger equation,

$$egin{aligned} H|\psi
angle &= E|\psi
angle\ E\psi &= -rac{\hbar^2}{2L}
abla^2\psi + rac{1}{2}L\omega^2Q^2\psi \end{aligned}$$



Creating Anharmonicity Superconductors – Foundations

Superconductors:

Discovered, 1911 by Kamerlingh Onnes.

Type-I superconductors:

Bardeen-Cooper-Schrieffer theory:

2 electrons form bound state (mediated by crystal lattice motion):

electron + electron + lattice => bound electron-electron state (Cooper-pair).

electron = fermion Cooper-pair = boson

Bosons:

Any number of bosons can occupy the same quantum state. => Perfect conductor in stability range: zero resistance, NO losses.



Superconductors – Temperature Range



Year

Superconductors – Macroscopic Effects Josephson Junction (JJ)



Tunneling of Cooper-pairs generates supercurrent.

Superconductors – Josephson Junctions Anharmonicity

Quantum LC Circuit:

- Equally spaced energies.
- Selection of well-defined qubits is impossible.

Anharmonic potential:

- NON-equal level spacing.
- Selection of unique qubit possible.



Superconductors – Macroscopic Effects Josephson Junctions

Anharmonic potential:

- NON-equal level spacing.
- Selection of unique qubit possible.

Sensitive to environmental Noise

"Buffer" with capacitor ("C").

Reduces anharmonicity.



Superconducting 1 Qubit Gates

Supercurrent Spins can bias with an external applied current.
can bias with external magnetic field.

$$H = \frac{\tilde{Q}(t)^2}{2C_{\Sigma}} + \frac{\Phi^2}{2L} + \frac{C_{\rm d}}{C_{\Sigma}} V_{\rm d}(t) \tilde{Q},$$

Superconducting Qubit/Transmon

Microwave drive

$$H = \underbrace{-\frac{\omega_{\mathbf{q}}}{2}\sigma_{z}}_{H_{0}} + \underbrace{\Omega V_{\mathbf{d}}(t)\sigma_{y}}_{H_{\mathbf{d}}}$$

(78)

 $\sigma_Z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$ $\sigma_Y = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}$

(74)

Krantz et al. (2019)

Superconducting 1 Qubit Gates

$$\widetilde{H}_{\rm d} = -\frac{\Omega}{2} V_0 s(t) \begin{pmatrix} 0 & e^{i(\delta\omega t + \phi)} \\ e^{-i(\delta\omega t + \phi)} & 0 \end{pmatrix}.$$
(90)

Superconducting gates are implemented in the time domain.

Consider the interaction part of the Hamiltonian:

$$\begin{pmatrix} 0 & e^{i(\delta\omega t + \phi)} \\ e^{-i(\delta\omega t + \phi)} & 0 \end{pmatrix} = \begin{pmatrix} 0 & A \\ B & 0 \end{pmatrix}$$

Logical operation: must have physical effect => |0> -> |1>, |1> -> |0>

Krantz et al. (2019)

Superconducting 2 Qubit Gates

Connecting TWO transmon qubits leads to a new interaction term:

$$H_{\rm qq} = g \left(\sigma^+ \sigma^- + \sigma^- \sigma^+ \right) = \frac{g}{2} \left(\sigma_x \sigma_x + \sigma_y \sigma_y \right). \quad (107)$$

Using time evolution, we can generate 2 qubit gates.

Superconducting 2 Qubit Gates

$$XY[t] = e^{-i\frac{g}{2}(\sigma_x\sigma_x + \sigma_y\sigma_y)t} = \begin{pmatrix} 1 & 0 & 0 & 0\\ 0 & \cos(gt) & -i\sin(gt) & 0\\ 0 & -i\sin(gt) & \cos(gt) & 0\\ 0 & 0 & 1 \end{pmatrix}$$

$$XY[\pi/2g] = iSWAP \equiv \begin{pmatrix} 1 & 0 & 0 & 0\\ 0 & 0 & -i & 0\\ 0 & -i & 0 & 0\\ 0 & 0 & 0 & 1 \end{pmatrix}$$

The $\sqrt{i \text{SWAP}}$ gate, which is equivalent to $XY[\frac{\pi}{4g}]$, is sometimes useful as well.

Ding and Chong (2020)

Superconducting 2 Qubit Gate



sequence of a several operations In time domain.

Ding and Chong (2020)

Quantum Processor



Quantum Information Science (QIS)

Dr. Boris Kiefer, Lecture 2

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Testing Superconducting Qubits; IBM-Q; CZ-Gate

Courtesy: Bryan Garcia (MS, NMSU Physics)



Both q_0 and q_1 are in the state $|0\rangle$ by default. In this case we see the state $|0\rangle$ regardless of which qubit we measure, since CZ only induces a phase flip.

 q_0

 q_1

Simulator (*Qasm_simulator*): 100% probability to measure |1>

Hardware

(*ibmq_16_melbourne*): about a 98% probability to measure |0>

Interested in Quantum Coding? See the IBM-Q developer page https://qiskit.org/

Testing Superconducting Qubits; IBM-Q; SWAP-Gate

Courtesy: Bryan Garcia (MS, NMSU Physics)



 q_0 is initialized in the state |1>, we apply a swap gate and measure q_1 . We indeed measure the state 1 after swapping

90

 q_1

Simulator (*Qasm_simulator*): 100% probability to measure |1> Hardware

(*ibmq_16_melbourne*): about a 91% probability to measure |1>

0.910

~

Interested in Quantum Coding? See the IBM-Q developer page https://qiskit.org/

Superconducting Qubits - 2013



2013: N~2000, crucial to reach stage 4: quantum error correction requires that qubits can be monitored at a rate faster than the occurring error.

Superconducting Qubits – 2019



H

2013: ~2000

10⁵ ns = 100 µs $\sim 10^4$ operations

2019: = 1000 µs $\sim 10^5$ operations

Cross-talk Noise reduction

Hamiltonian Engineering:

$$=\underbrace{-\frac{\omega_{\mathbf{q}}}{2}\sigma_{z}}_{H_{0}}+\underbrace{\Omega V_{\mathbf{d}}(t)\sigma_{y}}_{H_{\mathbf{d}}}$$

Kjaergaard et al. (2019)

Krantz et al. (2019)

Application Quantum Communication, Theory and Practice

Courtesy: Bryan Garcia (MS, NMSU Physics)

Courtesy: Bryan Garcia (MS, NMSU Physics)

• **Step a)** Random state to be teleported:

 $|q\rangle = a|0\rangle + b|1\rangle$

• Step b) Alice and Bob each hold a qubit of the entangled Bell state:

$$\begin{split} H \otimes |0\rangle &= \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle) \\ C_{not} \left(\frac{1}{\sqrt{2}} (|0\rangle + |1\rangle) \otimes |0\rangle \right) &= C_{not} \left(\frac{1}{\sqrt{2}} (|00\rangle + |10\rangle) \right) \\ |\psi\rangle &= \frac{1}{\sqrt{2}} (|00\rangle + |11\rangle) \end{split}$$
 Unentangled two-qubit state
 Entangled two-qubit Bell State

- Step c) Applying a CNOT gate followed by a Hadamard gate, the three-qubit entangled system becomes: $(H \otimes I \otimes I)(C_{not} \otimes I)(|q\rangle \otimes |\psi\rangle) = (H \otimes I \otimes I)(C_{not} \otimes I)\left(\frac{1}{\sqrt{2}} (a|000\rangle + a|011\rangle + b|100\rangle + b|111\rangle)\right)$ $= (H \otimes I \otimes I)\frac{1}{\sqrt{2}}(a|000\rangle + a|011\rangle + b|110\rangle + b|101\rangle)$ $= \frac{1}{2}(a(|000\rangle + |011\rangle + |100\rangle + |111\rangle) + b(|010\rangle + |001\rangle - |110\rangle - |101\rangle))$
- Step d & e) The state is separated into four states and sent to Bob, which he uses to decode:

$$= \frac{1}{2} (\begin{array}{ccc} |00\rangle\langle a|0\rangle + b|1\rangle\rangle \\ + |01\rangle\langle a|1\rangle + b|0\rangle\rangle \\ + |10\rangle\langle a|0\rangle - b|1\rangle\rangle \\ + |11\rangle\langle a|1\rangle - b|0\rangle) \end{array}) \xrightarrow{\text{Bob's State}} \begin{array}{c} \text{Bits Received} & \text{Gate Applied} \\ a|0\rangle + b|1\rangle\rangle & 00 & I \\ 0 & 1 & X \\ a|1\rangle + b|0\rangle\rangle & 01 & X \\ (a|1\rangle + b|0\rangle) & 01 & Z \\ (a|1\rangle - b|0\rangle) & 11 & ZX \end{array}$$

Team, T. (2020, December 14). Quantum Teleportation. Retrieved December 2020, from https://qiskit.org/textbook/ch-algorithms/teleportation.html#3.3-Using-the-QASM-Simulator-
 Rieffel, E., & Polak, W. (2014). Ch. 5/Quantum State Transformations. In *Quantum computing: A gentle introduction* (pp. 76-83). Cambridge, MA: The MIT Press.

Courtesy: Bryan Garcia (MS, NMSU Physics)

Fig.2 a) Qubit q_0 is initialized in a random state. b) We create a Bell state. c) q_0 is entangled with q_1 and q_2 . d) Alice measures and sends her qubits to Bob. e) Bob decodes qubits. f) Bob recovers Alice's original state, measures and stores in a classical register.



Qisket: Open-source IBM-Q experience.

[1] Team, T. (2020, December 14). Quantum Teleportation. Retrieved December 2020, from https://qiskit.org/textbook/ch-algorithms/teleportation.html#3.3-Using-the-QASM-Simulator-

Courtesy: Bryan Garcia (MS, NMSU Physics)

Simulator (Python based)



Simulator



Bob Measures the state |0> 100% percent of the time

Interested in Quantum Coding? See the IBM-Q developer page https://qiskit.org/

Courtesy: Bryan Garcia (MS, NMSU Physics)

Context:

- Linear/Chain Cluster States
- Teleportation Protocol (Johnston, 2019)



Approach: *n*-qubit GHZ_n state entangled with CZ gates^{Fig.) 2-Qubit Cluster State Teleportation Protocol Circuit [Wang, Li, Yin, Zq. *et al. (2018)*]}

Circuits:

• 2-Qubit Chain Cluster State (Huang et al., 2020)

Preliminary results:

- 2-Qubit Chain Cluster state Simulator: ($F \approx 99\%$)
- 2-Qubit Chain Cluster state Hardware: ($F \approx 85\%$)
- Compare to $F \approx 87\%$ (Huang et al, 2020)

Maximum classical fidelity: ~68% (Huang et al., 2020)



Fig.) Hardware: State Fidelities for a 2-Qubit Chain Cluster State

Courtesy: Bryan Garcia (MS, NMSU Physics)





Teleportation fidelity: Measure CORRELATION between Alice and Bob. Expected to be 100%.

Results: 6-qubit cluster state: 49%. 8-qubit cluster state: same. 10-qubit cluster state: same.

Maximum classical fidelity: ~68% (Huang et al., 2020)

At present, quantum teleportation inferior to classical transmission.

Quantum Sensing – A Primer

Quantum Sensing – Introduction

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Quantum Sensing

If energy levels are nearly equally spaced:

 \Rightarrow Initializing qubits is difficult/impossible.

Flipside:

Weak interactions can be resolved → excellent sensor for weak interactions/signals.



Quantum Sensing – Interference

Waves can interfere

- Amplify.
- Weaken.



constructive interference



partial destructive interference



complete destructive interference



https://flexbooks.ck12.org/cbook/ck-12-physics-flexbook-2.0/section/11.5/primary/lesson/wave-interference-ms-ps

Quantum Sensing – Matter Waves

De Broglie (1924)

The Nature of Light? Newton: Particle. Young: Wave. Einstein (photoelectric effect): Particle.



Particle: $E = mc^2$ E = pc

Wave: $c = \lambda f$ E = hf $E = hc/\lambda$

Combine: $\lambda = h/p$

https://www.metmuseum.org/art/collection/search/191811 https

https://www.aps.org/publications/apsnews/201010/physicshistory.cfm

Quantum Sensing – Matter Waves

Davisson and Germer (1925)

Electron beam on Ni target. Objective:

Study angular distribution of electrons emitted from the Ni target.

Vacuum failure → oxide formation → remove oxide at high temperatures.



Unintentional: Ni single crystal.

Quantum Sensing – Matter Waves

Davisson and Germer (1925)



Quantum Sensing – Gravity

First gravity measurement: Neutrons from nuclear reactor (immobile)

Neutrons are particles: Split into two beams.

A-C: slowing down, C-D, slow.C-D: longer wavelengthA-B: fast, B-D slowing down.B-D: shorter wavelength

=> Interference pattern CHANGES.



Figure 5.2 When the neutron interferometer is tilted so the upper path is raised higher, the effect of gravity influences the interference and causes the emerging neutrons to switch from detector C_3 to detector C_2 .

Alternating constructive/destructive interference: Repetition (angle) increment depends on local gravity.

Quantum Sensing – Gravity

The Gravitational Wave Spectrum



Quantum Sensing – Gravitational Waves, LIGO



Hanford: 0.007s delayed, distance = 2000km ⇒speed: v=distance/time =285714 km/s.

Within errorbar consistent with speed of light \Rightarrow Gravitational waves travel at speed of light \Rightarrow Gravitational waves are massless.



http://hyperphysics.phy-astr.gsu.edu/hbase/Forces/gravwav.html#c1

Quantum Sensing – Gravitational Waves, LIGO

Falling objects (kinematics):

 $t = \sqrt{2gh}$

Observation:

Time depends on gravity => changes in gravity can be measured using sensitive clocks.

Satellite:

Gravitational wave passes. Oscillatory change in gravity.







Quantum Sensing – Atomic Clocks



All atoms have identical energy levels

- \Rightarrow Energy for transition between energy levels are identical
- \Rightarrow Frequency of emitted/absorbed photons is identical.
- \Rightarrow Ideal clocks/time keepers.

Quantum Sensing – Gravitational Waves



Satellite: Gravitational wave passes. Oscillatory change in gravity.

Noise?!? Reduce by using three satellites.

https://www.google.com/search?q=satellites+quantum+kasevitch&tbm=isch&ved=2ahUKEwiXm9_IhoPvAhUBcs0KHYrSCTUQ2cCegQIABAA&oq=satellites+quantum+kasevitch&gs_lcp=CgNpbWcQA1CvggFYpJoBYOGbAWgAcAB4AIAB2wGIAfENkgEFMC45LjGYAQCgAQGqAQtnd3Mtd2l6LWltZ8ABAQ&sclient=img&ei=h402YNe7OoHktQaKpaeoAw&bih=667&biw=13 &rlz=1C1CHBF_enUS811US811#imgrc=pRQ_nv1UzBOqzM

Summary

- QIS Overview.
- Review of Core Concepts:

Quantum States; Superposition; Measurement; Entanglement.

- Some Types of Quantum Hardware.
- Quantum LC Circuit: Equally Spaced Energy levels.
- Superconductivity: A Quantum State of Matter:

Fundamentals.

Josephson Junction.

NON-Equally Spaced Energy Levels.

Summary

- Transmon: IBM, Google,...
- Superconducting 1 Qubit Gates.
- Superconducting 2 Qubit Gates: CNOT + Entanglement.
- Qisket: Testing of Superconducting Qubits on IBM-Q.
- Quantum Communication (courtesy: Bryan Garcia, NMSU Physics).
 Teleportation.
 - Qisket Implementation:
 - Divergence theory and practice.
 - At present: generally superconducting teleportation
 - implementation inferior to classical information processing.

Summary

- Quantum Sensing.
- De Broglie relationship; wave matter duality.
- Atomic clocks.
- Gravitational waves.

This is an exciting time, with many new opportunities for quantum enabled technologies.

QIS Efforts Kiefer Research Group

Quantum hardware:

 2D Materials, topological materials, fault tolerant quantum computing.

Discovery of novel solid state qubits.

• Molecular qubits for quantum computing.

 Improving superconducting qubits, transmons.



Unperturbed





Microwaves: 0.1 – 10 cm⁻¹ (0.01– 1 eV)

QIS Efforts Kiefer Research Group

Quantum software:

- Cluster states.
- IBM-Q hardware testing.
- Next: SNL, ion traps hardware testing.



QIS Workforce Development

What is a path forward in Quantum Skilled Workforce Development?

What would you like to see? What would help you to consider a QIS career?

Quantum Information Science (QIS)

Quantum Computing Quantum Communication Quantum Sensing

This is an exciting time, with many new opportunities for quantum enabled technologies.

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